

Gravitinos, Reheating and the Matter-Antimatter Asymmetry of the Universe

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OUTLINE

- THE MATTER-ANTIMATTER ASYMMETRY OF THE UNIVERSE
- INFLATION AND REHEATING
- THE GRAVITINO PROBLEM, AND T_{reh}
REHEATING, GRAVITINOS AND THE M-A ASYMMETRY
- SOLUTIONS TO THE GRAVITINO PROBLEM
- GRAVITINO PROBLEM AGAIN
- CONCLUSION

MATTER-ANTIMATTER ASYMMETRY OF THE UNIVERSE

- **SOLAR SYSTEM** — PROBES, INTERACTION OF SOLAR WIND WITH PLANETS
- **MILKY WAY** — COSMIC RAYS
- **CLUSTER (20 Mpc)** — GALACTIC COLLISIONS
INTERGALACTIC HOT PLASMA
- **UP TO 1000 Mpc** — COSMIC DIFFUSE GAMMA
RAY SPECTRUM

(ANNIHILATIONS AT BOUNDARY FROM $z=1000$ TO 20 – 380,000
YR TO 100 MILLION YR)

(Cohen, de Rujula, Glashow)³

MATTER-ANTIMATTER ASYMMETRY OF THE UNIVERSE

- ANTIMATTER RULED OUT TILL $d \sim 1000$ Mpc
- SIZE OF OBSERVABLE UNIVERSE $\sim ct_U = 4000$ Mpc

$$(1 \text{ Mpc} = 3 \times 10^{19} \text{ km} = 3 \times 10^6 \text{ lt-yr})$$

MATTER-ANTIMATTER ASYMMETRY OF THE UNIV

MATTER-ANTIMATTER ASYMMETRY

- EARLY TIMES ($t < 1 \text{ s} = \text{PRIM. NUCL.}$) EQUAL AMOUNTS OF MATTER AND ANTIMATTER
- WHY THIS ASYMMETRY TODAY? WHERE DID THE ANTIMATTER GO?

MATTER-ANTIMATTER ASYMMETRY

- EARLY TIMES ($t < 1$ s = PRIM. NUCL.) EQUAL AMOUNTS OF MATTER AND ANTIMATTER
- WHY THIS ASYMMETRY TODAY? WHERE DID THE ANTIMATTER GO?
- DISEQUILIBRIUM IN THE EARLY UNIVERSE
 $100 M + 100 A \rightarrow 103 M + 101 A \rightarrow 2 M$



$r_M > r_A$, GET MORE MATTER THAN ANTIMATTER

MATTER-ANTIMATTER ASYMMETRY

- X = GUT GAUGE/HIGGS BOSONS
 - GUT BARYOGENESIS MASS ($M_X \sim 10^{16}$ GeV)
- X = HEAVY RIGHT HANDED MAJORANA NEUTRINOS
 - **LEPTOGENESIS** MODELS
 - MASS ($M_N \sim 10^{10}$ GeV)

1 GeV = PROTON MASS

MATTER-ANTIMATTER ASYMMETRY

WHEREFROM

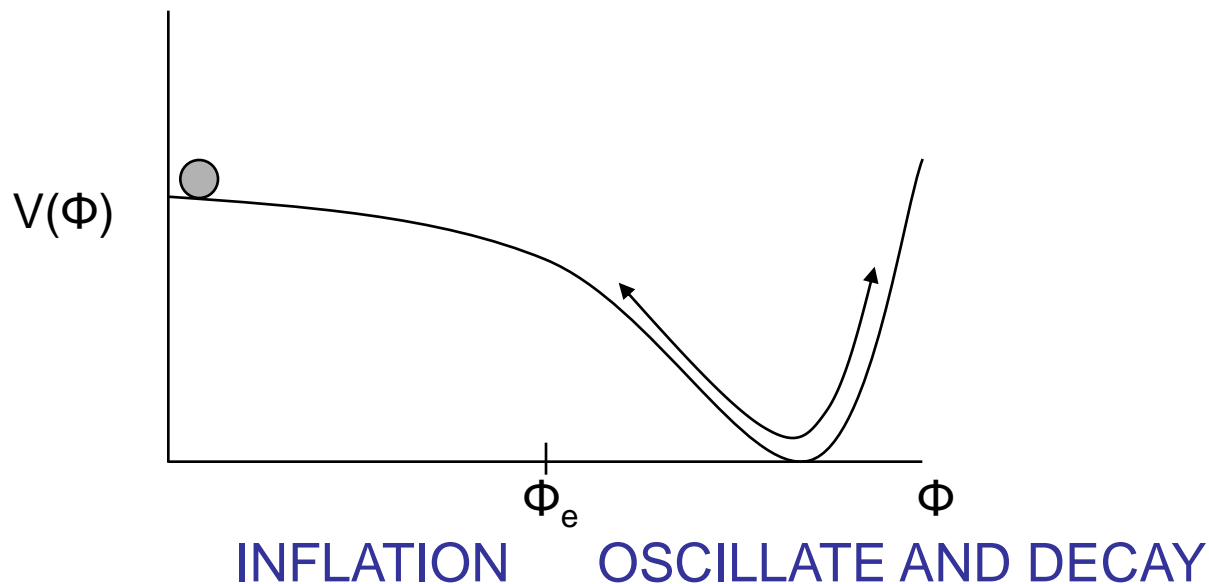
- GUT GAUGE/HIGGS BOSONS ($M_X \sim 10^{16}$ GeV)
- HEAVY RIGHT HANDED MAJORANA NEUTRINOS
($M_N \sim 10^{10}$ GeV) ?

1 GeV = PROTON MASS

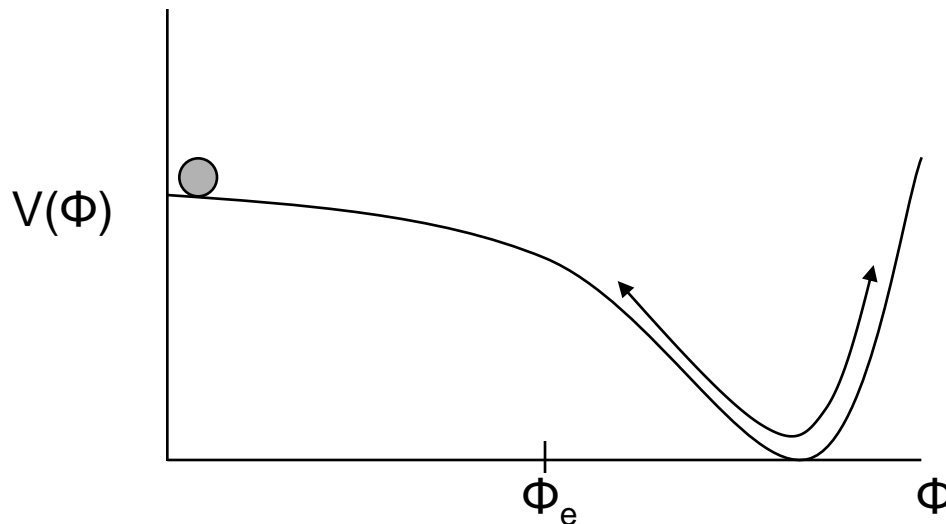
INFLATION and REHEATING

INFLATION – PERIOD OF ACCELERATED EXPANSION
IN THE EARLY UNIVERSE ($t \sim 10^{-38}$ s or later)

ASSOCIATED WITH THE DYNAMICS OF A SLOWLY
VARYING FIELD CALLED THE INFLATON Φ



INFLATION and REHEATING



INFLATION OSCILLATE AND DECAY (REHEATING)

DURING INFLATION, $R \sim \exp(H t)$ [R IS THE SCALE FACTOR,
 $d(t) = d_i R(t)$]

n OF ALL SPECIES $\rightarrow 0$

INFLATON DECAY PRODUCTS THERMALISE, T_{reh}
THERMAL BATH HAS q, l, H, dm , BSM INCLUDING GUT
PARTICLES AND HEAVY NEUTRINOS

REHEATING

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GRAVITINOS

\tilde{G} = SUPERSYMMETRIC PARTNER OF THE GRAVITON

SUPERSYMMETRY

- EXTENSION OF THE STANDARD MODEL (GAUGE HIERARCHY)
- SUPERPARTNERS: FERMION – BOSON

PHOTON – PHOTINO, ELECTRON – SELECTRON
(EQUAL m , IF SUSY)

LOCAL SUPERSYMMETRY: SUPERGRAVITY

GRAVITON – GRAVITINO (\tilde{G})

BROKEN ($m_{\tilde{G}}$: eV – TeV)

GRAVITINOS

\tilde{G} = SUPERSYMMETRIC PARTNER OF THE GRAVITON

PRODUCED AFTER INFLATION $t \sim 10^{-38}$ s ($m_{\tilde{G}} : \text{eV} - \text{TeV}$)

COSMOLOGICAL CONSEQUENCES (m, n)

- STABLE : AFFECTS EXPANSION RATE, $\rho_{\tilde{G}} > \rho_c$ (L/H)
- UNSTABLE : AFFECT EXPANSION RATE PRIOR TO DECAY

DECAY PRODUCTS $\rho > \rho_c$

DESTROY LIGHT ELEMENTS ${}^4\text{He}, {}^3\text{He}, D$
(NUCLEOSYNTHESIS)

GRAVITINO PROBLEM(S)

GRAVITINOS

\tilde{G} = SUPERSYMMETRIC PARTNER OF THE GRAVITON

PRODUCED AFTER INFLATION $t \sim 10^{-34}$ s ($m_{\tilde{G}} : \text{eV} - \text{TeV}$)

COSMOLOGICAL CONSEQUENCES (m, n)

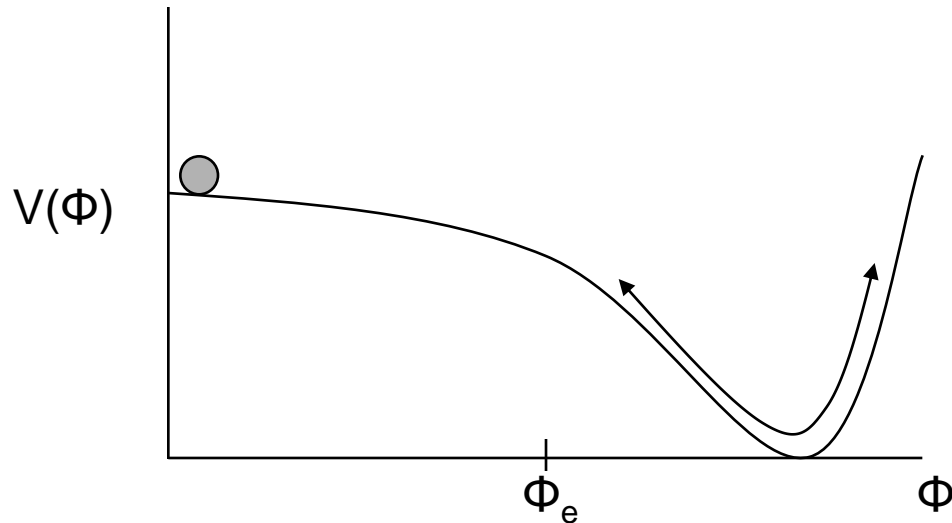
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DESTROY LIGHT ELEMENTS ${}^4\text{He}, {}^3\text{He}, D$
(NUCLEOSYNTHESIS)

GRAVITINO PROBLEM(S) => UPPER BOUND ON $\rho_{\tilde{G}} \propto n_{\tilde{G}}$

STANDARD PICTURE OF GRAVITINO PRODUCTION



INFLATION → REHEATING (OSC. + DECAY) (T_{reh})

→ RADIATION DOMINATED UNIV
(Relativistic particles)

THERMAL SCATTERING → \tilde{G}
(gluons, quarks, squarks, gluinos) 15

STANDARD CALC OF GRAVITINO PRODUCTION

CALCULATE GRAVITINO PRODUCTION IN THE RAD DOM ERA

MAINLY PRODUCED AT THE BEGINNING OF THE RAD DOM ERA
WHEN $T \sim T_{\text{reh}}$, AND $n_{\tilde{G}} \propto T_{\text{reh}}$.

UPPER BOUND ON $n_{\tilde{G}}$

⇒ UPPER BOUND ON T_{reh} OF $10^6\text{--}9$ GeV (MASS 100 GeV – 10 TeV)

$$1 \text{ GeV} = 10^{13} \text{ K}$$

REHEATING, GRAVITINOS AND MATTER-ANTIMATTER ASYMMETRY

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- THE UPPER BOUND ON THE REHEAT TEMPERATURE 10^{6-9} GeV TO SUPPRESS GRAVITINO PRODUCTION

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- MATTER-ANTIMATTER ASYMMETRY GENESIS MODELS REQUIRE HEAVY X, MASS 10^{10} , 10^{16} GeV

REHEATING, GRAVITINOS AND MATTER-ANTIMATTER ASYMMETRY

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- MATTER-ANTIMATTER ASYMMETRY GENESIS MODELS REQUIRE HEAVY X, MASS 10^{10} , 10^{16} GeV

DIFFICULT TO HAVE ENOUGH HEAVY X IN THE RADIATION DOMINATED UNIV AFTER REHEATING

$$n_X \sim \exp(- m c^2/k_B T)$$

REHEATING, GRAVITINOS AND MATTER-ANTIMATTER ASYMMETRY

- THE UPPER BOUND ON THE REHEAT TEMPERATURE 10^{6-9} GeV TO SUPPRESS GRAVITINO PRODUCTION
- MATTER-ANTIMATTER ASYMMETRY GENESIS MODELS REQUIRE HEAVY X, MASS 10^{10} , 10^{16} GeV

DIFFICULT TO HAVE ENOUGH HEAVY X IN THE RADIATION DOMINATED UNIV AFTER REHEATING

LOW REHEAT TEMPERATURE IS A PROBLEM FOR GUT BARYOGENESIS AND LEPTOGENESIS

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SOLUTIONS

WE FOCUS ON **LEPTOGENESIS** MODELS –
OUT OF EQM DECAY OF N .

POPULAR – RELATED TO LIGHT NEUTRINO MASSES

MASS $M_N \sim 10^{10}$ GeV

SOLUTIONS

PROBLEM: TWO SPECIES NEUTRINOS AND GRAVITINOS

BOTH CREATED IN THE SAME THERMAL ENVIRONMENT

-- RADIATION DOMINATED UNIVERSE AFTER REHEATING

WANT N (M-A ASYMMETRY) BUT NOT \tilde{G}

CAN INCREASE N

OR

SUPPRESS \tilde{G}

SOLUTIONS

INCREASE N

RESONANCE LEPTOGENESIS

SOFT LEPTOGENESIS

PREHEATING (WORKS FOR GUT BARYOGENESIS TOO)

DETAILED VIEW OF REHEATING

DECREASE \tilde{G}

**DELAYED THERMALISATION DURING REHEATING
DUE TO SUSY FLAT DIRECTIONS**

SUSY FLAT DIRECTIONS

STANDARD MODEL , H SCALAR (SPIN 0)

SCALAR POTENTIAL IN SUSY IS A FUNCTION OF

$$(H_u, H_d, \tilde{q}_i, \tilde{l}_i)$$

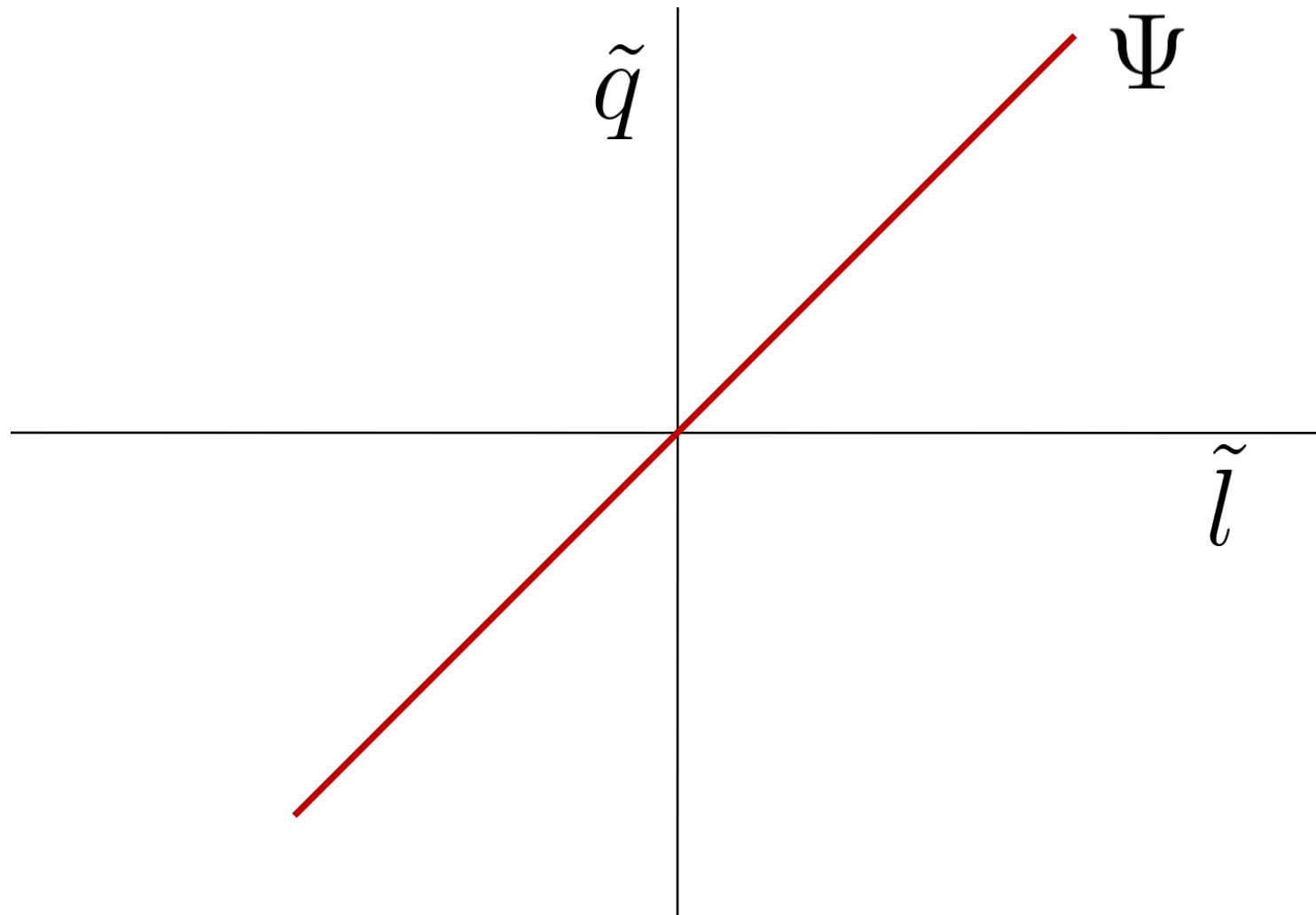
DIRECTIONS IN FIELD SPACE OF SCALARS ALONG WHICH THE SCALAR POTENTIAL VANISHES

— **FLAT DIRECTIONS**

UDD: $\langle \tilde{u}_L \rangle = \psi, \langle \tilde{s}_L \rangle = \psi, \langle \tilde{b}_L \rangle = \psi$ PHASES

REPRESENTED BY A FIELD Ψ (AFFLECK-DINE FIELD) WITH VEV ψ

SUSY FLAT DIRECTIONS



COSMOLOGICAL CONSEQUENCES

NON-ZERO VALUE OF ψ GIVES MASS TO GAUGE BOSONS (BREAKS GAUGE SYMMETRY),

e.g.,

$$L \supset \tilde{q}^* \tilde{q} A A$$

COSMOLOGICAL CONSEQUENCES

NON-ZERO VALUE OF ψ GIVES MASS TO GAUGE BOSONS (BREAKS GAUGE SYMMETRY),

e.g., $L \supset \tilde{q}^* \tilde{q} A A$

IF ALL GAUGE BOSONS GET MASS [LLddd, QuQue], IT SLOWS DOWN THERMALISATION AFTER INFLATION.

SUPPRESSES GRAVITINO PRODUCTION

ALLAHVERDI AND MAZUMDAR

(FLAT DIRECTION DECAYS BEFORE EWSB $t \sim 10^{-11}$ s)

COSMOLOGICAL CONSEQUENCES

GRAVITINOS PRODUCED BY SCATTERING OF INFLATON DECAY PRODUCTS

$n_{\tilde{G}}$ DEPENDS ON n OF SCATTERERS

STANDARD PICTURE:

INFLATON DECAYS $\rightarrow n_0 \rightarrow$ THERMALISE
KINETIC EQM n_0
CHEMICAL EQM n_1

FLAT DIRECTIONS THAT BREAK ALL GAUGE SYMM

INFLATON DECAYS $\rightarrow n_0 \rightarrow$ DELAYED THERMALISATION

$$n \sim n_0 \ll n_1 \quad [10^4]$$

DILUTE PLASMA, $n_{\tilde{G}} \downarrow\downarrow$ $N \downarrow$

RESULTS

SUPPRESSED GRAVITINO PRODUCTION DUE TO

A) DILUTE PLASMA

B) PHASE SPACE SUPPRESSION

$$q + \bar{\tilde{q}} \rightarrow g + \tilde{G} \quad q + \bar{q} \rightarrow \tilde{g} + \tilde{G} \quad \tilde{q} + \bar{\tilde{q}} \rightarrow \tilde{g} + \tilde{G}$$

OUTGOING GLUON/GLUINO HEAVY

GRAVITINO PRODUCTION SHUTS OFF WHEN THE ENERGY OF INCOMING QUARKS/SQUARKS $< m_{g,\tilde{g}}$

RESULTS

SUPPRESSED GRAVITINO PRODUCTION DUE TO

A) DILUTE PLASMA

B) PHASE SPACE SUPPRESSION

$$Y_{\tilde{G}} = 4 \times 10^{-18}, 10^{-20} < 10^{-14}$$

COMPLETE SHUT OFF

PRODUCTION AFTER THE FLAT DIRECTION DECAYS
IS NOT LARGE $\propto T_f$ [10^5 GeV] [RR, A. SARKAR] 32

ALTERNATE SCENARIO WITH SUSY FLAT DIRECTIONS

- **GRAVITINO OVER-PRODUCTION**

GRAVITINO PROBLEM AGAIN!

- IF A FLAT DIRECTION GIVES MASS TO SOME BUT NOT ALL GAUGE BOSONS, THERMALISATION WILL OCCUR
- CONSIDERED SUCH A FLAT DIRECTION [H_u H_d]

PHOTONS, GLUONS AND PHOTINOS AND GLUINOS
LIGHT

QUARKS AND SQUARKS HEAVY

$$\tilde{g} + q \longrightarrow \tilde{q}^* \longrightarrow \tilde{G} + q$$

GRAVITINO PROBLEM AGAIN!

$$\tilde{g} + q \longrightarrow \tilde{q}^* \longrightarrow \tilde{G} + q$$

- RESONANT PRODUCTION OF GRAVITINOS WHEN

$$E_{\tilde{g}} + E_q \approx m_{\tilde{q}}$$

- GRAVITINO ABUNDANCE GENERATED IS VERY LARGE AND GREATER THAN THE COSMOLOGICAL UPPER BOUND FOR MOST PARAMETER SPACE

GRAVITINO PROBLEM AGAIN!

$$\tilde{g} + q \longrightarrow \tilde{q}^* \longrightarrow \tilde{G} + q$$

- RESONANT PRODUCTION OF GRAVITINOS WHEN

$$E_{\tilde{g}} + E_q = m_{\tilde{q}}$$

- GRAVITINO ABUNDANCE GENERATED IS VERY LARGE AND GREATER THAN THE COSMOLOGICAL UPPER BOUND FOR MOST PARAMETER SPACE
- COSMOLOGICAL UPPER BOUND IS $Y < 10^{-14}$
- FOR DIFFERENT SETS OF PARAMETERS

$$Y = 10^{-8} \text{ — } 10^{-2}$$

GRAVITINO PROBLEM AGAIN!

- LARGE VALUES FOR SUSY FLAT DIRECTIONS IS GENERIC. EXACERBATED GRAVITINO PROBLEM
- HAVE TO INVOKE EARLY DECAY OF FLAT DIRECTIONS TO AVOID CONFLICT

CONCLUSION

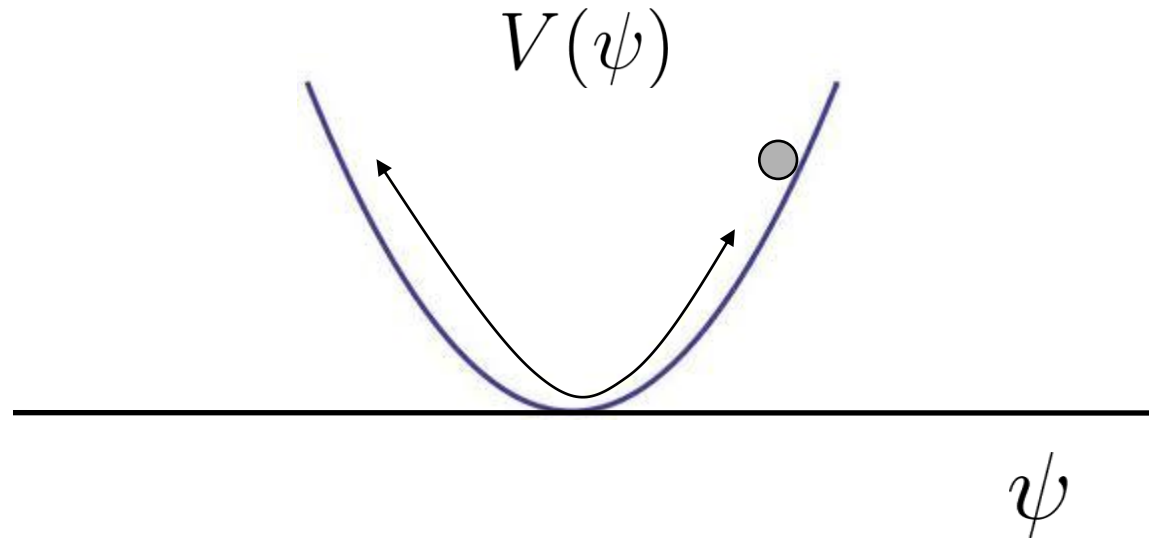
1. POPULAR MODELS OF GENERATING THE MATTER-ANTIMATTER ASYMMETRY OF THE UNIVERSE REQUIRE A LARGE REHEAT TEMPERATURE AFTER INFLATION
2. BUT THAT GENERATES TOO MANY GRAVITINOS IN THE UNIVERSE
3. COSMOLOGISTS ARE LOOKING FOR MECHANISMS TO ENHANCE NEUTRINO ABUNDANCE/SUPPRESS GRAVITINO ABUNDANCE

CONCLUSION

4. GRAVITINO ABUNDANCE GENERATED IN A NON-THERMAL UNIVERSE IN THE PRESENCE OF FLAT DIRECTIONS IS SUPPRESSED
5. GRAVITINO ABUNDANCE IN A THERMAL UNIVERSE WITH FLAT DIRECTIONS CAN BE LARGE – NEW SOURCE OF THE GRAVITINO PROBLEM

(DETAILS OF SUSY MODEL)

SUSY FLAT DIRECTIONS



FLAT DIRECTION \rightarrow QUADRATIC POT WITH CURV m_0

$\psi_0 \neq 0$ DUE TO QUANTUM FLUCTUATIONS DURING INFLATION; OTHER REASONS

WHEN $H \sim m_0$, Ψ OSCILLATES, $\psi \sim 1/R^{3/2}$

THEN IT DECAYS

(BEFORE t_{EW})

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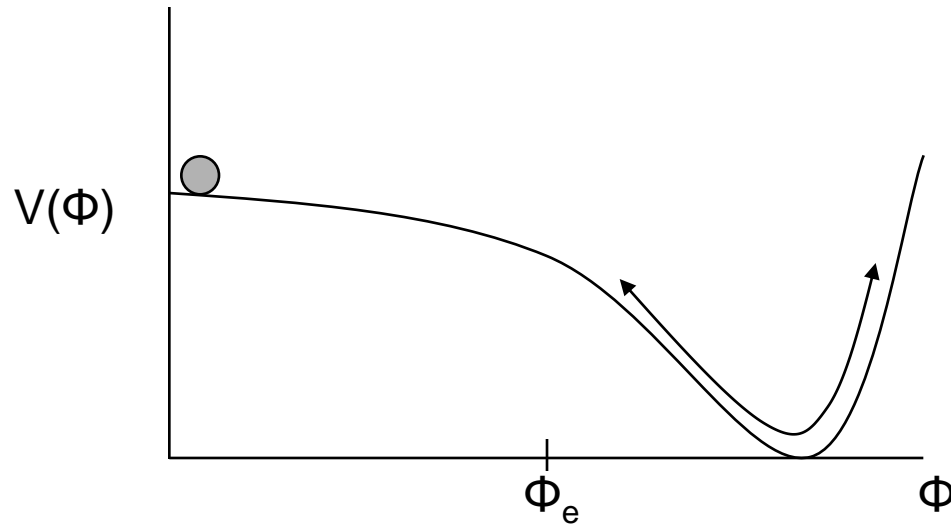
with N. Sahu, A. Sarkar, N. Mahajan

SOLUTION 1

INCREASE N

DETAILED VIEW OF REHEATING

UPTIL NOW ASSUMED INSTANTANEOUS INFLATON DECAY AND REHEATING.



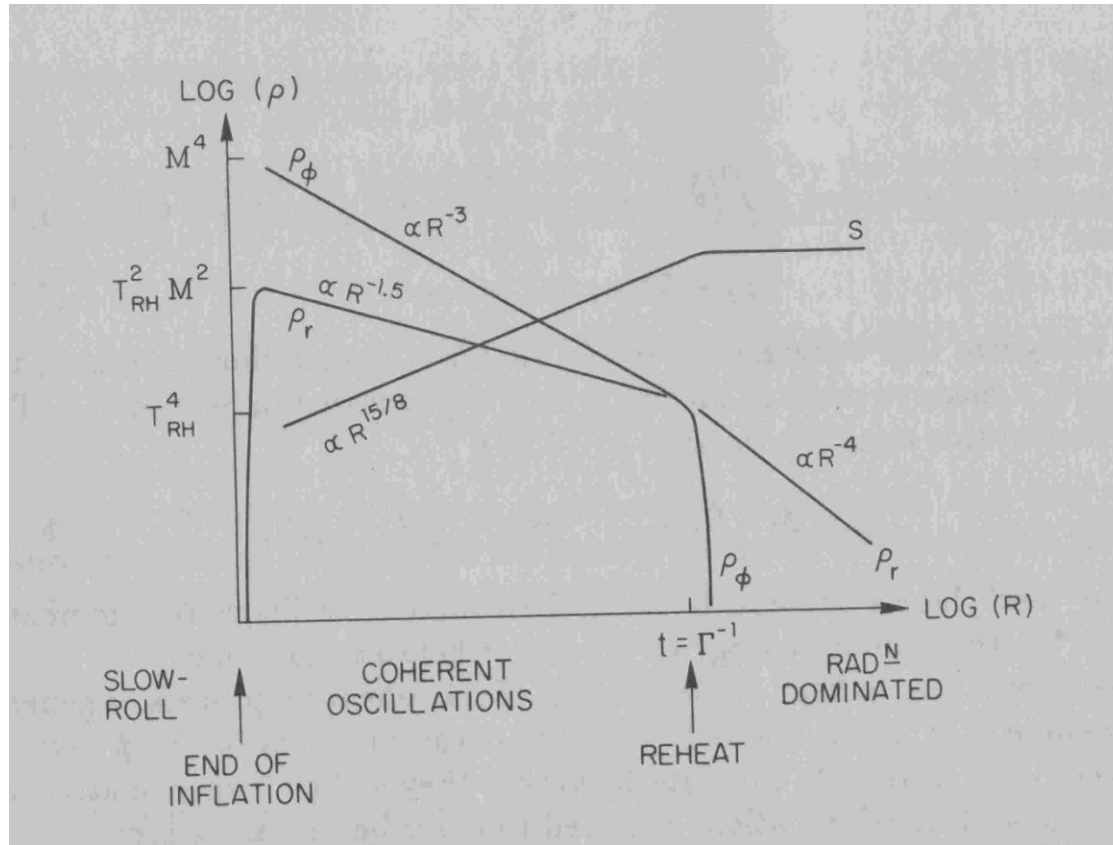
INFLATON OSCILLATES. AT $t = \Gamma_{\phi}^{-1}$, $T : 0 \rightarrow T_{\text{reh}}$

T_{reh} IS INITIAL AND MAX TEMP OF RAD DOM ERA

$T_{\text{reh}} < M_N$ PROBLEM FOR LEPTOGENESIS

STANDARD CALC OF N PRODUCTION ALSO ASSUMES INSTANTANEOUS INFLATON DECAY AND REHEATING.

QUADRATIC
INFLATON
POTENTIAL
DURING
REHEATING



$$\rho_r \propto T^4$$

$$T \rightarrow T_{\max} \rightarrow T_{\text{reh}}$$

KOLB & TURNER

T_{reh} IS THE FINAL TEMPERATURE AT THE END OF REHEATING

THE SOLUTION

T_{\max} CAN BE AS HIGH AS $1000 T_{\text{reh}}$

SO SUFFICIENT NUMBER OF HEAVY RIGHT-HANDED
NEUTRINOS (N) WITH $M_N \sim 10 T_{\text{reh}}$ CAN BE PRODUCED
DURING REHEATING

CHUNG ET AL, DELEPINE AND SARKAR, GIUDICE ET AL

IF T_{\max} CAN ENHANCE NEUTRINO PRODUCTION, CAN IT ALSO
ENHANCE GRAVITINO PRODUCTION ?

IF $n_{\tilde{G}}(\text{RAD DOM ERA}) \propto T_{\text{reh}}$ (MAX TEMP OF RAD DOM ERA),

WILL $n_{\tilde{G}}(\text{REHEATING ERA}) \propto T_{\max}$?

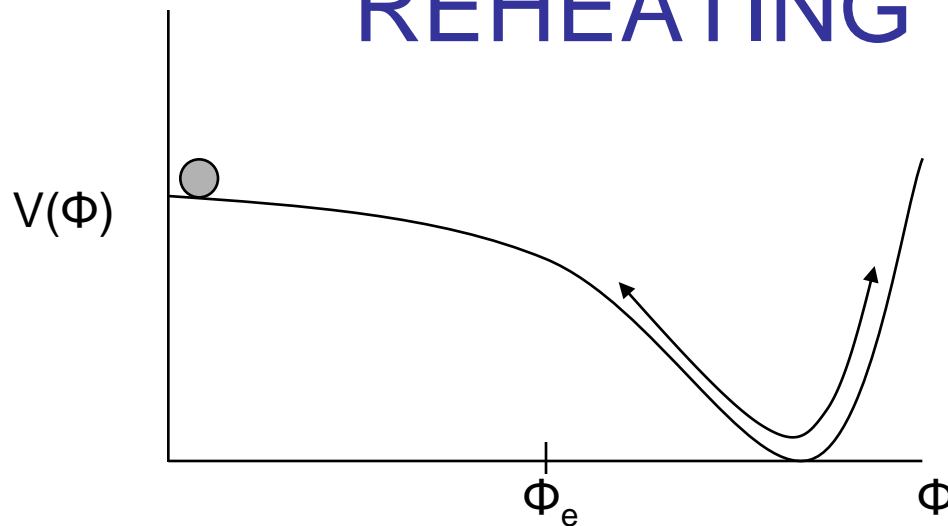
IF $n_{\tilde{G}}(\text{REH}) \gg n_{\tilde{G}}(\text{RD})$, GET BOUNDS ON T_{\max}

-- THEN THE PROBLEM FOR LEPTOGENESIS CAN REAPPEAR

CALCULATE $n_{\tilde{G}}(\text{REH})$

- EXPECT $n_{\tilde{G}}(T_{\text{MAX}})$
- $n_{\tilde{G}}(\text{REH}) >, < n_{\tilde{G}}(\text{RD})$

GRAVITINO PRODUCTION DURING REHEATING



INFLATON DECAYS AND DECAY PRODUCTS
THERMALISE QUICKLY $\Rightarrow T(t)$

$$\frac{dn_{\tilde{G}}}{dt} + 3Hn_{\tilde{G}} = \langle \Sigma_{\text{tot}} |v| \rangle n^2$$

$$\dot{T} \frac{dn_{\tilde{G}}}{dT} + 3Hn_{\tilde{G}} = \langle \Sigma_{\text{tot}} |v| \rangle n^2$$

$$\frac{dn_{\tilde{G}}}{dt} + 3Hn_{\tilde{G}} = \langle \Sigma_{\text{tot}} |v| \rangle n^2$$

$H =$ HUBBLE PARAMETER (DILUTION DUE TO EXPANSION)

$\Sigma_{\text{tot}} =$ TOTAL CROSS SECTION FOR GRAVITINO PRODUCTION

$v =$ RELATIVE VELOCITY OF THE INCOMING PARTICLES

$\langle \quad \rangle$ THERMAL AVERAGING

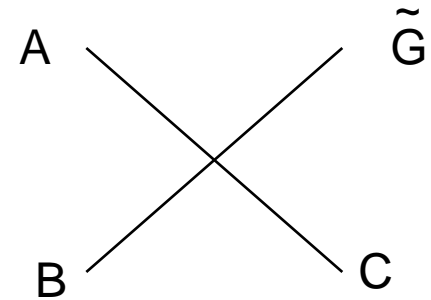
$n = \frac{1.2}{\pi^2} T^3$ NUMBER DENSITY OF SCATTERERS

IGNORED DECAY $\tau \sim 10^{7-8} (100\text{GeV}/m_{\tilde{G}}) \text{ s}$

FOR $m_{\tilde{G}} \sim 100\text{GeV}, \tau \sim 1 \text{ yr}$ DECAY NOT RELEVANT⁴⁹

CALCULATION OF $\langle \Sigma_{\text{tot}} | v \rangle$

\tilde{G} PRODUCED BY THE SCATTERING OF INFLATON DECAY PRODUCTS



e.g. $q + \bar{q} \rightarrow g + \tilde{G}$

$q + \bar{q} \rightarrow \tilde{g} + \tilde{G}$

$\tilde{q} + \bar{\tilde{q}} \rightarrow \tilde{g} + \tilde{G}$

$$\langle \Sigma_{\text{tot}} | v \rangle = \alpha / M_{Pl}^2$$

PRADLER AND STEFFEN

$$G_N = 1 / M_{Pl}^2$$

$$\dot{T} \frac{dn_{\tilde{G}}}{dT} + 3Hn_{\tilde{G}} = \langle \Sigma_{\text{tot}} |v| \rangle n^2$$

$$\rho_r \sim R^{-\frac{3}{2}} \Rightarrow T \sim R^{-\frac{3}{8}} \sim t^{-1/4} \quad [\text{R IS THE SCALE FACTOR}]$$

$$R \sim t^{\frac{2}{3}}$$

SOLVE FROM T_{max} TO T_{reh} .

$$n_{\tilde{G}}(T_{\text{reh}}) = 0.007 \frac{\alpha}{M_{Pl}^2} \frac{T_{\text{max}}^4 T_{\text{reh}}^2}{H_{\text{max}}} \quad \text{for } T_{\text{max}} \gg T_{\text{reh}}$$

$$Y_{\tilde{G}}(T_{\text{reh}}) = \frac{n_{\tilde{G}}(T_{\text{reh}})}{s(T_{\text{reh}})} = 0.01 g_{\text{reh}}^{-1} \frac{\alpha}{M_{Pl}^2} \frac{T_{\text{max}}^4}{H_{\text{max}} T_{\text{reh}}}$$

RESULTS

INCLUDE GRAVITINO PRODUCTION IN THE RAD DOM ERA
FROM T_{reh} TO T_f . SOLVE BOLTZMANN EQN IN RD ERA.

$$Y_{\tilde{G}}(T_f) = Y_{\tilde{G}}(T_{\text{reh}}) + 0.02 g_{\text{reh}}^{-3/2} \frac{\alpha}{M_{Pl}} T_{\text{reh}} \quad T_f \ll T_{\text{reh}}$$

EARLIER $Y_{\tilde{G}}(T_{\text{reh}})$ SET TO 0

$$Y_{\tilde{G}}(T_f) = 0.03 g_{\text{reh}}^{-1} \frac{\alpha}{M_{Pl}^2} \left[0.4 \frac{T_{\text{max}}^4}{H_{\text{max}} T_{\text{reh}}} + 0.6 g_{\text{reh}}^{-\frac{1}{2}} M_{Pl} T_{\text{reh}} \right]$$

$$T_{\max} \simeq 0.8 g_*^{-\frac{1}{4}} M_I^{\frac{1}{2}} (\Gamma_\phi M_{Pl})^{\frac{1}{4}}$$

$$M_I = \text{SCALE OF INFLATION} \leq 10^{16} \text{ GeV} \quad \rho_\phi = M_I^4$$

$$\Gamma_\phi = \text{DECAY RATE OF THE INFLATON}$$

$$g_* = \text{NUMBER OF REL. DEG. OF FREEDOM} \sim 230 \text{ IN MSSM}$$

$$T_{\text{reh}} \simeq 0.55 g_{*\text{reh}}^{-\frac{1}{4}} (M_{Pl} \Gamma_\phi)^{\frac{1}{2}}$$

$$H_{\max} \simeq \sqrt{\frac{8\pi}{3}} \frac{M_I^2}{M_{Pl}}$$

KOLB AND TURNER

2 INDEPENDENT VARIABLES

$$Y_{\tilde{G}}(T_f) = 0.03 g_{\text{reh}}^{-1} \frac{\alpha}{M_{Pl}^2} \left[0.4 \frac{T_{\text{max}}^4}{H_{\text{max}} T_{\text{reh}}} + 0.6 g_{\text{reh}}^{-\frac{1}{2}} M_{Pl} T_{\text{reh}} \right]$$

$$H_{\text{max}} = 2.0 g_*^{\frac{1}{2}} \frac{T_{\text{max}}^4}{T_{\text{reh}}^2 M_{Pl}}$$

$$Y_{\tilde{G}}(T_f) = 0.007 g_{\text{reh}}^{-3/2} \frac{\alpha}{M_{Pl}} [T_{\text{reh}} + 3.0 T_{\text{reh}}]$$

- DEPENDENCE ON T_{max} CANCELS OUT [UNEXPECTED]

$$Y_{\tilde{G}}(T_f) = 0.03 g_{\text{reh}}^{-1} \frac{\alpha}{M_{Pl}^2} \left[0.4 \frac{T_{\text{max}}^4}{H_{\text{max}} T_{\text{reh}}} + 0.6 g_{\text{reh}}^{-\frac{1}{2}} M_{Pl} T_{\text{reh}} \right]$$

$$H_{\text{max}} = 2.0 g_*^{\frac{1}{2}} \frac{T_{\text{max}}^4}{T_{\text{reh}}^2 M_{Pl}}$$

$$Y_{\tilde{G}}(T_f) = 0.007 g_{\text{reh}}^{-3/2} \frac{\alpha}{M_{Pl}} [T_{\text{reh}} + 3.0 T_{\text{reh}}]$$

- DEPENDENCE ON T_{max} CANCELS OUT [UNEXPECTED]
- GRAVITINO PRODUCTION DURING REHEATING IS COMPARABLE (1/3) TO THAT IN THE RADIATION DOMINATED ERA [UNEXPECTED]

COMPARISON WITH NUMERICAL ANALYSIS

KAWASAKI, KOHRI AND MOROI

NUMERICAL FIT TO FINAL

$$Y_{\tilde{G}} \simeq 1.9 \times 10^{-12} \times \left(\frac{T_{\text{reh}}}{10^{10} \text{ GeV}} \right) \\ \times \left[1 + 0.045 \ln \left(\frac{T_{\text{reh}}}{10^{10} \text{ GeV}} \right) \right] \left[1 - 0.028 \ln \left(\frac{T_{\text{reh}}}{10^{10} \text{ GeV}} \right) \right]$$

SAME FUNCTIONAL FORM

GIUDICE, RIOTTO AND TKACHEV: SIMILAR RELATIVE MAGNITUDES

IMPLICATIONS FOR LEPTOGENESIS

NO LARGE ENHANCEMENT IN TOTAL GRAVITINO
PRODUCTION

CHANGE IN THE BOUND ON THE REHEAT
TEMPERATURE (FACTOR OF 4/3)

$$T_{\max} \sim T_{\text{reh}}^{\frac{1}{2}}$$

NO NEW CONSTRAINTS ON T_{\max} DUE TO
GRAVITINO PRODUCTION DURING REHEATING

SO NOT AFFECT SCENARIO OF PRODUCTION OF
HEAVY NEUTRINOS DURING REHEATING

SOLUTION 2

DECREASE \tilde{G}

**DELAYED THERMALISATION DURING REHEATING
DUE TO SUSY FLAT DIRECTIONS**

SUSY FLAT DIRECTIONS

STANDARD MODEL , H SCALAR (SPIN 0)

$\langle H \rangle \neq 0 \Rightarrow q, l, W, Z$ GET MASS

IN SUPERSYMMETRIC STANDARD MODEL, HAVE

$$H_u, H_d, \tilde{q}_i, \tilde{l}_i$$

FOR SOME COMB. OF THESE SCALARS, THEIR INITIAL VALUE IN THE EARLY UNIVERSE AFTER INFLATION, NEED NOT BE 0 (Q FLUC, OTHER)

$$\langle \tilde{u} \rangle = \psi, \quad \langle \tilde{s} \rangle = \psi, \quad \langle \tilde{b} \rangle = \psi \quad \text{FLAT DIR}$$

ψ DECREASES IN TIME, AND THEN DISAPPEARS
(FLAT DIRECTION DECAY, BEFORE EWSB)

EARLIER INFLATON DECAYS AND DECAY PRODUCTS THERMALISE QUICKLY

$$q + \bar{q} \rightarrow g + \tilde{G} \quad q + \bar{q} \rightarrow \tilde{g} + \tilde{G} \quad \tilde{q} + \bar{\tilde{q}} \rightarrow \tilde{g} + \tilde{G}$$

$$\dot{n}_{\tilde{G}} + 3Hn_{\tilde{G}} = \langle \Sigma_{\text{tot}} |v| \rangle n^2 \quad n \sim T^3$$

NOW,
$$\dot{n}_{\tilde{G}} + 3Hn_{\tilde{G}} = \int d\Pi_1 d\Pi_2 f_1 f_2 W_{12}(s)$$

$f_{1,2}$ PARTICLE DISTRIBUTION FUNCTIONS FOR
INCOMING PARTICLES

$$W_{12}(s) \propto \sigma_{CM}$$

$$q + \bar{q} \rightarrow g + \tilde{G} \quad q + \bar{q} \rightarrow \tilde{g} + \tilde{G} \quad \tilde{q} + \bar{\tilde{q}} \rightarrow \tilde{g} + \tilde{G}$$

- DISTRIBUTION FUNCTIONS

$$f_i = C_i \delta \left(E_i - \frac{m_I}{2} \frac{R_d}{R} \right) \quad \text{for } t_d < t < t_{kin}$$

$$= \exp \left(-\frac{E_i - \xi_i}{T} \right) \quad \text{for } t_{kin} < t < t_{thr}$$

- PHASE SPACE SUPPRESSION

OUTGOING GAUGE BOSON/ GAUGINO HEAVY
 GRAVITINO PRODUCTION SHUTS OFF WHEN THE
 ENERGY OF INCOMING QUARKS/SQUARKS $< m_{g, \tilde{g}^1}$

- SO FAR SEEN TWO SOLUTIONS OF THE GRAVITINO PROBLEM – INCREASING NEUTRINO, SUPPRESSING GRAVITINO

- **ALTERNATE SCENARIO**

ALTERNATE SCENARIO

- IF FLAT DIRECTION VEV DOES NOT BREAK ALL GAUGE SYMMETRIES, THERMALISATION WILL OCCUR
- CONSIDER A SCENARIO WITH $H_u H_d$ FLAT DIRECTION. $SU(3)_C \times SU(2)_L \times U(1)_Y \rightarrow SU(3)_C \times U(1)_{EM}$
- QUARK AND SQUARK HEAVY (NR), $m \approx h\psi$
$$m_{\tilde{q}}^2 - m_q^2 = m_S^2 \quad m_S^2 \sim T^2 \ll m_{q,\tilde{q}}^2$$
- GLUINOS LIGHT ($m \sim gT$, REL), THERMAL DISTRIBUT.

GRAVITINO PROBLEM AGAIN!

$$\tilde{g} + q \longrightarrow \tilde{q}^* \longrightarrow \tilde{G} + q$$

- RESONANT PRODUCTION OF GRAVITINOS AS SQUARK CAN GO ON SHELL
- GRAVITINO ABUNDANCE GENERATED IS VERY LARGE AND GREATER THAN THE COSMOLOGICAL UPPER BOUND FOR MOST PARAMETER SPACE
- COSMOLOGICAL UPPER BOUND IS $Y < 10^{-14}$
- FOR DIFFERENT SETS OF PARAMETERS

$$Y = 10^{-8} \text{ — } 10^{-2}$$

GRAVITINO PROBLEM AGAIN!

- LARGE VEVS FOR SUSY FLAT DIRECTIONS IS GENERIC. EXACERBATED GRAVITINO PROBLEM
- HAVE TO INVOKE EARLY DECAY OF FLAT DIRECTIONS TO AVOID CONFLICT

CONCLUSION

4. NEUTRINOS GENERATED DURING REHEATING ~ GRAVITINO ABUNDANCE GENERATED NOT TOO LARGE
5. GRAVITINO ABUNDANCE GENERATED IN A NON-THERMAL UNIVERSE IN THE PRESENCE OF FLAT DIRECTIONS IS SUPPRESSED
6. GRAVITINO ABUNDANCE IN A THERMAL UNIVERSE WITH FLAT DIRECTIONS CAN BE LARGE – NEW SOURCE OF THE GRAVITINO PROBLEM (DETAILS OF SUSY MODEL)

OUTLINE

- THE MATTER-ANTIMATTER ASYMMETRY OF THE UNIVERSE
- INFLATION AND REHEATING
- THE GRAVITINO PROBLEM, AND T_{reh}

REHEATING, GRAVITINOS AND THE M-A ASYMMETRY

- A WAY OUT: **DETAILED VIEW OF REHEATING**
- ANOTHER WAY OUT: **DELAYED THERMALISATION**
- **GRAVITINO PROBLEM AGAIN**

CONCLUSION

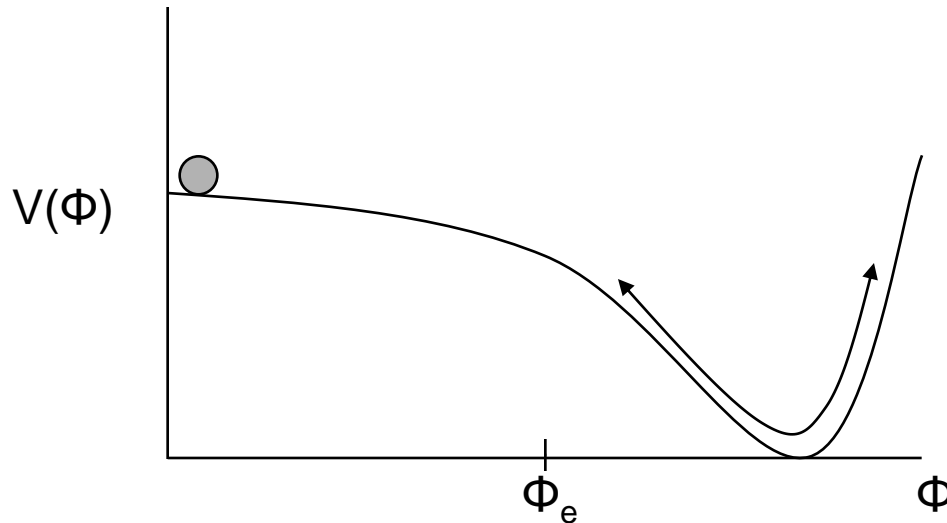
REHEATING, GRAVITINOS AND MATTER-ANTIMATTER ASYMMETRY

- THE UPPER BOUND ON THE REHEAT TEMPERATURE 10^{6-9} GeV TO SUPPRESS GRAVITINO PRODUCTION
- MATTER-ANTIMATTER ASYMMETRY GENESIS MODELS REQUIRE HEAVY X, MASS 10^{10} , 10^{16} GeV

DIFFICULT TO PRODUCE HEAVY X
IN THE RAD DOMINATED UNIV AFTER REHEATING

LOW REHEAT TEMPERATURE IS A PROBLEM FOR
GUT BARYOGENESIS AND LEPTOGENESIS

SUMMARY OF THE PROBLEM



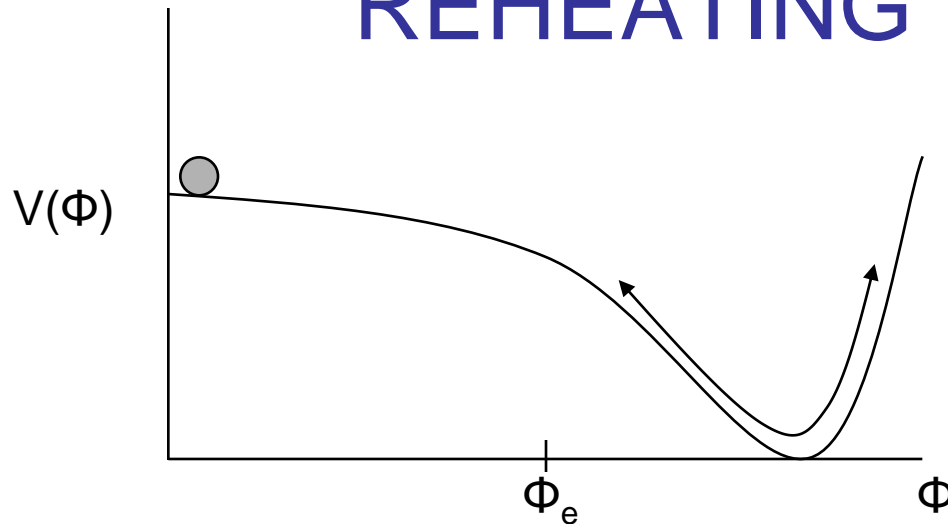
INFLATION \rightarrow REHEATING (T_{reh})

\rightarrow RADIATION DOMINATED UNIV

THERMAL SCATTERING $\rightarrow \tilde{G}$
 $\rightarrow N$

UPPER BOUND ON T_{reh} TO SUPPRESS \tilde{G} SUPPRESSES N TOO 70

GRAVITINO PRODUCTION DURING REHEATING



INFLATON DECAYS AND DECAY PRODUCTS
THERMALISE QUICKLY

$$\frac{dn_{\tilde{G}}}{dt} + 3Hn_{\tilde{G}} = \langle \Sigma_{\text{tot}} |v| \rangle n^2$$

$$\frac{dn_{\tilde{G}}}{dt} + 3Hn_{\tilde{G}} = \langle \Sigma_{\text{tot}} |v| \rangle n^2$$

$H =$ HUBBLE PARAMETER (DILUTION DUE TO EXPANSION)

$\Sigma_{\text{tot}} =$ TOTAL CROSS SECTION FOR GRAVITINO PRODUCTION

$v =$ RELATIVE VELOCITY OF THE INCOMING PARTICLES

$\langle \quad \rangle$ THERMAL AVERAGING

$n = \frac{1.2}{\pi^2} T^3$ NUMBER DENSITY OF SCATTERERS

IGNORED DECAY $\tau \sim 10^{7-8} (100\text{GeV}/m_{\tilde{G}}) \text{ s}$

FOR $m_{\tilde{G}} \sim 100\text{GeV}, \tau \sim 1 \text{ yr}$ DECAY NOT RELEVANT⁷²

QUARTIC POTENTIAL

- REDONE FOR A QUARTIC POTENTIAL $R \sim t^{1/2}$
- $H(T), \rho_\phi(T), \rho_r(T)$ DIFFERENT

$$Y_{\tilde{G}}(\text{REH}) = \frac{1}{2} Y_{\tilde{G}}(\text{RD})$$

CONCLUSION

- OBTAINED AN ANALYTIC EXPRESSION FOR GRAVITINO PRODUCTION DURING REHEATING
- THE ABUNDANCE IS OF THE SAME ORDER AS THAT DURING THE RADIATION DOMINATED ERA (THE STANDARD CALC)
- THE DEPENDENCE ON T_{\max} CANCELS OUT
- NO NEW CONSTRAINTS ON LEPTOGENESIS MODELS INVOKING T_{\max}

$$\dot{T} \frac{dn_{\tilde{G}}}{dT} + 3Hn_{\tilde{G}} = \langle \Sigma_{\text{tot}} |v| \rangle n^2$$

$$n \sim T^3, \quad \text{NEED } \dot{T} \text{ AND } H(T)$$

QUADRATIC INFLATON POTENTIAL DURING REHEATING, $R \sim t^{\frac{2}{3}}$

$$\rho_r \sim R^{-\frac{3}{2}} \Rightarrow T \sim R^{-\frac{3}{8}} \sim t^{-1/4} \quad [\text{R IS THE SCALE FACTOR}]$$

$$\dot{T} = -\frac{3}{8}TH_{\text{max}} \left(\frac{T}{T_{\text{max}}} \right)^4$$

$$H = \frac{\dot{R}}{R} = -\frac{8\dot{T}}{3T} = H_{\text{max}} \left(\frac{T}{T_{\text{max}}} \right)^4 .$$

$$\dot{T} \frac{dn_{\tilde{G}}}{dT} + 3Hn_{\tilde{G}} = \langle \Sigma_{\text{tot}} |v| \rangle n^2$$

$$n \sim T^3, \quad \text{NEED } \dot{T} \text{ AND } H(T)$$

QUADRATIC INFLATON POTENTIAL DURING REHEATING, $R \sim t^{\frac{2}{3}}$

$$\rho_r \sim R^{-\frac{3}{2}} \Rightarrow T \sim R^{-\frac{3}{8}} \sim t^{-1/4} \quad [\text{R IS THE SCALE FACTOR}]$$

SOLVE FROM T_{max} TO T_{reh} .

$$n_{\tilde{G}}(T_{\text{reh}}) = 0.007 \frac{\alpha}{M_{Pl}^2} \frac{T_{\text{max}}^4 T_{\text{reh}}^2}{H_{\text{max}}} \quad \text{for } T_{\text{max}} \gg T_{\text{reh}}$$

$$Y_{\tilde{G}}(T_{\text{reh}}) = \frac{n_{\tilde{G}}(T_{\text{reh}})}{s(T_{\text{reh}})} = 0.01 g_{\text{reh}}^{-1} \frac{\alpha}{M_{Pl}^2} \frac{T_{\text{max}}^4}{H_{\text{max}} T_{\text{reh}}}$$

$$\dot{T} \frac{dn_{\tilde{G}}}{dT} + 3Hn_{\tilde{G}} = \langle \Sigma_{\text{tot}} |v| \rangle n^2$$

$$\dot{T}, H(T), n \sim T^3$$

$$T \sim R^{-\frac{3}{8}} \quad R \sim t^{\frac{2}{3}} \quad [\text{R IS THE SCALE FACTOR}]$$

SOLVE FROM T_{max} TO T_{reh} .

$$n_{\tilde{G}}(T_{\text{reh}}) = 0.007 \frac{\alpha}{M_{Pl}^2} \frac{T_{\text{max}}^4 T_{\text{reh}}^2}{H_{\text{max}}} \quad \text{for } T_{\text{max}} \gg T_{\text{reh}}$$

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IMPLICATIONS FOR LEPTOGENESIS

NO LARGE ENHANCEMENT IN TOTAL GRAVITINO PRODUCTION

THOUGH $T_{\max} \gg T_{\text{reh}}$, AND $n_{\tilde{G}}(REH) < n_{\tilde{G}}(RD)$

- NO LARGE CHANGE IN THE BOUND ON THE REHEAT TEMPERATURE

UPPER BOUND ON T_{reh} OF 10^{6-9}GeV GOES DOWN BY 4/3

- $T_{\max} \sim T_{\text{reh}}^{\frac{1}{2}}$ SO NOT AFFECT PRODUCTION OF HEAVY

NEUTRINOS AT T_{\max}

GRAVITINO PRODUCTION

- **DETAILED VIEW OF REHEATING**

$N \uparrow \uparrow$ BUT $\tilde{G} \uparrow$

- **DELAYED THERMALIZATION IN THE PRESENCE OF SUSY FLAT DIRECTIONS**

SUSY FLAT DIRECTIONS

SCALAR POTENTIAL IN SUSY IS A FUNCTION OF
 $(\tilde{q}, \tilde{l}, H_u, H_d)$

DIRECTIONS IN FIELD SPACE OF SCALARS ALONG WHICH THE SCALAR POTENTIAL VANISHES

$$\langle \tilde{u} \rangle = \psi, \quad \langle \tilde{s} \rangle = \psi, \quad \langle \tilde{b} \rangle = \psi \quad \text{PHASES}$$

CALLED FLAT DIRECTIONS AS THE POTENTIAL IS FLAT AS YOU VARY THE VALUE OF ψ

INITIAL VALUE NEED NOT BE 0 (Q FLUC, OTHER)
 ψ DECREASES IN TIME, AND THEN DISAPPEARS
(DECAYS) ⁸⁰

SUSY FLAT DIRECTIONS

SUSY BREAKING LIFTS THE POTENTIAL OF Ψ
– GIVES MASS TO THE FIELD

INITIAL VALUE OF THE FIELD MAY BE AWAY
FROM 0

WHEN $H < m_\psi$ THE FIELD OSCILLATES IN ITS
POTENTIAL

FINALLY Ψ DECAYS, GAUGE SYMMETRIES
RESTORED

COSMOLOGICAL CONSEQUENCES

NON-ZERO VALUE OF THE FIELD Ψ GIVES
MASS TO GAUGE BOSONS, e.g.,

$$L \supset \tilde{q}^* \tilde{q} A A$$

COSMOLOGICAL CONSEQUENCES

NON-ZERO VALUE OF THE FIELD Ψ GIVES
MASS TO GAUGE BOSONS, e.g.,

$$L \supset \tilde{q}^* \tilde{q} A A$$

IF ALL GAUGE SYMMETRIES BROKEN [LLddd,
QuQue], IT SLOWS DOWN THERMALISATION
AFTER INFLATION.

DILUTE PLASMA. AFFECTS GRAVITINO
PRODUCTION

ALLAHVERDI AND MAZUMDAR

EARLIER INFLATON DECAYS AND DECAY PRODUCTS THERMALISE QUICKLY

$$q + \bar{q} \rightarrow g + \tilde{G} \quad q + \bar{q} \rightarrow \tilde{g} + \tilde{G} \quad \tilde{q} + \bar{\tilde{q}} \rightarrow \tilde{g} + \tilde{G}$$

$$\dot{n}_{\tilde{G}} + 3Hn_{\tilde{G}} = \langle \Sigma_{\text{tot}} |v| \rangle n^2 \quad n \sim T^3$$

NOW,
$$\dot{n}_{\tilde{G}} + 3Hn_{\tilde{G}} = \int d\Pi_1 d\Pi_2 f_1 f_2 W_{12}(s)$$

$$W_{12}(s) = 4p_{12} \sqrt{s} \sigma_{CM}(s)$$

$$p_{12} = [s - (m_1 + m_2)^2]^{1/2} [s - (m_1 - m_2)^2]^{1/2} / [2\sqrt{s}]$$

$$s = (E_1 + E_2)_{CM}^2$$

- FLAT DIRECTION HAS A LARGE INITIAL VEV (DURING INFLATION)
- AFTER INFLATION, LARGE GAUGE BOSON MASS, SLOWS DOWN THERMALISATION
 DELAYED t_{KIN}
 DELAYED t_{CHEM}
- VEV DECREASES AND FINALLY FLAT DIRECTION DECAYS AT t_f .

GAUGE SYMMETRIES RESTORED ($t_f \ll t_{\text{EW}}$)

RESULTS

- $m_0 = 100 \text{ GeV} < \Gamma_\psi = 10^4 \text{ GeV}, \quad t_0 > t_d$

NO GRAVITINO PRODUCTION EVEN AFTER THERMALISATION TILL THE FLAT DIRECTIONS DECAYS, DUE TO PHASE SPACE SUPPRESSION

PRODUCTION AFTER THE FLAT DIRECTION DECAYS IS STANDARD $\propto T_f$ [10⁵ GeV]

LOW

RESULTS

- $m_0 = 100 \text{ GeV} > \Gamma_\psi = 10 \text{ GeV}, \quad t_0 < t_d$

SUPPRESSED GRAVITINO PRODUCTION TILL
THERMALISATION

$$Y_{\tilde{G}} = 4 \times 10^{-18}, 10^{-20} < 10^{-14}$$

NO GRAVITINO PRODUCTION AFTER
THERMALISATION TILL THE FLAT DIRECTION DECAYS

PRODUCTION AFTER THE FLAT DIRECTION DECAYS IS
NOT LARGE $\propto T_f [10^5 \text{ GeV}]$

GRAVITINO PROBLEM AGAIN!

$$\tilde{g} + q \longrightarrow \tilde{q}^* \longrightarrow \tilde{G} + q$$

- RESONANT PRODUCTION OF GRAVITINOS AS SQUARK CAN GO ON SHELL
- GRAVITINO ABUNDANCE GENERATED IS VERY LARGE AND GREATER THAN THE COSMOLOGICAL UPPER BOUND FOR MOST PARAMETER SPACE

GRAVITINO PROBLEM AGAIN!

$$\tilde{g} + q \longrightarrow \tilde{q}^* \longrightarrow \tilde{G} + q$$

- RESONANT PRODUCTION OF GRAVITINOS AS SQUARK CAN GO ON SHELL
- GRAVITINO ABUNDANCE GENERATED IS VERY LARGE AND GREATER THAN THE COSMOLOGICAL UPPER BOUND FOR MOST PARAMETER SPACE
- COSMOLOGICAL UPPER BOUND IS $Y < 10^{-14}$
- FOR DIFFERENT SETS OF PARAMETERS

$$Y = 10^{-8} \text{ — } 10^{-2}$$

RESULTS

- GRAVITINO ABUNDANCE SUPPRESSED
- LEPTOGENESIS IN THE NON-THERMAL UNIVERSE?

DILUTE PLASMA AFFECTS NUMBER DENSITY OF
HEAVY RIGHT HANDED NEUTRINOS TOO

BUT SUFFICIENT TO CREATE REQUIRED BARYON
ASYMMETRY

ALLAHVERDI AND MAZUMDAR

CONCLUSION

1. GRAVITINO ABUNDANCE GENERATED DURING REHEATING \sim ABUNDANCE GENERATED AFTERWARDS
2. GRAVITINO ABUNDANCE GENERATED IN A NON-THERMAL UNIVERSE IN THE PRESENCE OF FLAT DIRECTIONS IS SUPPRESSED
3. GRAVITINO ABUNDANCE IN A THERMAL UNIVERSE WITH FLAT DIRECTIONS CAN BE LARGE

CONCLUSION

4. NEUTRINOS GENERATED DURING REHEATING ~ GRAVITINO ABUNDANCE GENERATED NOT TOO LARGE (WITH SOME UNEXPECTED RESULTS)
5. GRAVITINO ABUNDANCE GENERATED IN A NON-THERMAL UNIVERSE IN THE PRESENCE OF FLAT DIRECTIONS IS SUPPRESSED (NEW CAUSES)
6. GRAVITINO ABUNDANCE IN A THERMAL UNIVERSE WITH FLAT DIRECTIONS CAN BE LARGE – NEW SOURCE OF THE GRAVITINO PROBLEM